Cambridge
International
AS \& A Level

## Cambridge International Examinations

Cambridge International Advanced Subsidiary and Advanced Level

## MATHEMATICS

 9709/06Paper 6
MARK SCHEME
Maximum Mark: 50
$\square$

## Mark Scheme Notes

Marks are of the following three types:
M Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.

A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).

B Mark for a correct result or statement independent of method marks.

- When a part of a question has two or more "method" steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly when there are several B marks allocated. The notation DM or DB (or dep*) is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.
- The symbol $\sqrt{ }$ implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only. A and B marks are not given for fortuitously "correct" answers or results obtained from incorrect working.
- Note: B2 or A2 means that the candidate can earn 2 or 0. B2/1/0 means that the candidate can earn anything from 0 to 2.

The marks indicated in the scheme may not be subdivided. If there is genuine doubt whether a candidate has earned a mark, allow the candidate the benefit of the doubt. Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored.

- Wrong or missing units in an answer should not lead to the loss of a mark unless the scheme specifically indicates otherwise.
- For a numerical answer, allow the A or B mark if a value is obtained which is correct to 3 s.f., or which would be correct to 3 s.f. if rounded ( 1 d.p. in the case of an angle). As stated above, an A or B mark is not given if a correct numerical answer arises fortuitously from incorrect working. For Mechanics questions, allow A or B marks for correct answers which arise from taking g equal to 9.8 or 9.81 instead of 10.

The following abbreviations may be used in a mark scheme or used on the scripts:

| AEF | Any Equivalent Form (of answer is equally acceptable) |
| :--- | :--- |
| AG | Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid) |
| BOD | Benefit of Doubt (allowed when the validity of a solution may not be absolutely clear) |
| CAO | Correct Answer Only (emphasising that no "follow through" from a previous error is allowed) |
| CWO | Correct Working Only - often written by a 'fortuitous' answer |
| ISW | Ignore Subsequent Working |
| MR | Misread |
| PA | Premature Approximation (resulting in basically correct work that is insufficiently accurate) |
| SOSSee Other Solution (the candidate makes a better attempt at the same question) |  |

SR Special Ruling (detailing the mark to be given for a specific wrong solution, or a case where some standard marking practice is to be varied in the light of a particular circumstance)

## Penalties

MR-1 A penalty of MR-1 is deducted from $A$ or $B$ marks when the data of a question or part question are genuinely misread and the object and difficulty of the question remain unaltered. In this case all A and B marks then become "follow through $\sqrt{ }$ " marks. MR is not applied when the candidate misreads his own figures - this is regarded as an error in accuracy. An MR -2 penalty may be applied in particular cases if agreed at the coordination meeting.

PA -1 This is deducted from A or B marks in the case of premature approximation. The PA -1 penalty is usually discussed at the meeting.

| Question | Answer | Marks | Partial Marks | Guidance |
| :---: | :---: | :---: | :---: | :---: |
| 1 | $\begin{aligned} & p=0.76 \\ & \mathrm{P}(\text { fewer than } 10)=1-\mathrm{P}(10,11) \end{aligned}$ | 1 | M1 | Any binomial term |
|  | $=1-(0.76)^{10}(0.24)^{11} \mathrm{C}_{10}-(0.76)^{11}$ | 1 | M1 | ${ }^{11} \mathrm{C}_{x} p^{x}(1-p)^{I l-x}, 0<p<1$ |
|  | $=1-0.219$ | 1 | M1 | Any binomial term ${ }^{n} \mathrm{C}_{x}(0.76)^{x}(0.24)^{n-x}$ |
|  | $=0.781$ | 1 | A1 | $1-\mathrm{P}(10,11)$ oe binomial expression Correct answer |
|  |  | 4 |  |  |
| 2 | $\mu=54.1$ | 1 | B1 | Stated or evaluated |
|  | $z=-1.11$ | 1 | B1 | Accept rounding to $\pm 1.1$ |
|  | $-1.11=\frac{50.9-54.1}{\sigma}$ | 1 | M1 | Standardising no cc no sq rt |
|  | $\sigma=2.88$ | 1 | A1 | Correct answer |
|  |  | 4 |  |  |
| 3(i) | $a=9 / \mathrm{cw}$ |  | M1 | Using $\mathrm{fd}=\mathrm{f} / \mathrm{cw}$ |
|  | $=9 / 2=4.5$ |  | A1 | Correct $a$ |
|  | $1.5=b / 4$ so $b=6$ |  | A1 | Correct $b$ |
|  |  | [3] |  |  |

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| Question | Answer | Marks | Partial Marks | Guidance |
| :---: | :---: | :---: | :---: | :---: |
| 3(ii) |  | 1 | B1 $\sqrt{ }$ ' | Correct heights ft their $b$ |
|  |  | 1 | B1 | Correct widths, ie 3, 2, 3, 4 starting either 60 or 59.5 |
|  |  | 1 | B1 | Labels fd, time or minutes and squiggle and bars from 59.5 to 71.5 |
|  |  | 3 |  |  |
| 4(i) | $\bar{x}=80-147 / 30=80-4.9$ | 1 | M1 | For $-147 / 30$ oe seen |
|  | $=75.1$ | 1 | A1 | Correct answer |
|  | sd $=\sqrt{ }\left(\frac{952}{30}-\left(\frac{147}{30}\right)^{2}\right)=\sqrt{ } 7.72 \ldots$ | 1 | M1 | $952 / 30-( \pm \text { their coded mean })^{2}$ |
|  | sd $=2.78$ | 1 | A1 | Correct answer |
|  | 4 |  |  |  |


| Question | Answer | Marks | Partial Marks | Guidance |
| :---: | :---: | :---: | :---: | :---: |
| 4(ii) | $\mathrm{P}(x>160)=\mathrm{P}\left(z>\frac{160-148.6}{18.5}\right)$ | 1 | M1 | Standardising no cc no sq rt |
|  | $\begin{aligned} & =\mathrm{P}(z>0.616) \\ & =1-0.7310 \end{aligned}$ | 1 | M1 | $1-\Phi$ |
|  | $=0.269$ | 1 | A1 | Correct answer |
|  |  | 3 |  |  |
| 5(i) | 5 (i) eg **(EEEE) ${ }^{* * *}$ | 1 | M1 | Mult by 6! Oe |
|  | $\text { Number of ways }=\frac{6!}{2!2!}=180$ | 2 | $\begin{aligned} & \text { M1 } \\ & \text { A1 } \end{aligned}$ | Dividing by $2!2$ ! oe Correct answer |
|  |  | 3 |  |  |
| 5(ii) | $\mathrm{S}^{* * * * * * * \mathrm{~T}}$ or $\mathrm{T}^{* * * * * * * S}$ | 1 | M1 | Mult by 7 ! Or dividing by one of 2 ! or 4! |
|  | Number of ways $=\frac{7!}{4!2!} \times 2$ | 1 | M1 | Mult by 2 |
|  | $=210$ | 1 | A1 | Correct answer |
|  |  | 3 |  |  |


| Question | Answer |  |  |  |  |  | Marks | Partial Marks | Guidance |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 5(iii) | exactly one E in ${ }^{6} \mathrm{C}_{3}$ ways |  |  |  |  | 2 |  | $\begin{array}{\|l\|} \hline \text { M1 } \\ \text { M1 } \end{array}$ | ${ }^{6} \mathrm{C}_{x}$ as a single answer <br> ${ }^{x} \mathrm{C}_{3}$ as a single answer |
|  | $=20$ |  |  |  |  | 1 |  | A1 | correct answer |
|  |  |  |  |  |  | 3 |  |  |  |
| 6(i) |  |  |  |  |  | 1 |  | M1 | 3 pairs S (bank, $\log$ in, success oe) and F oe seen no extra bits. |
|  |  |  |  |  |  | 1 |  | A1 | Exactly 3 pairs, must be labelled |
|  |  |  |  |  |  | 1 |  | A1 | Correct diagram with all probs correct |
|  |  |  |  |  |  |  | 3 |  |  |
| 6(ii) | $\begin{array}{\|l\|} \hline x \\ \hline \text { Prob } \\ \hline \end{array}$ | 0 |  |  | 3 | 1 |  | B1 | $\mathrm{P}(0)$ correct |
|  |  | 0.4 |  | 0.144 | 0.216 | 1 |  | M1 | Multiplying two of more factors of 0.4 and 0.6 |
|  |  |  |  |  |  | 1 |  | A1 | One more correct prob |
|  |  |  |  |  |  | 1 |  | B1 | One more correct prob |
|  |  |  |  |  |  | 4 |  |  |  |


| Question | Answer | Marks | Partial Marks | Guidance |
| :---: | :---: | :---: | :---: | :---: |
| 6(iii) | $\mathrm{E}(X)=0.24+2 \times 0.144+3 \times 0.216$ | 1 | M1 | Using $\Sigma p_{i} x_{i}$ |
|  | $=1.176$ (1.18) | 1 | A1 | Correct answer |
|  |  | 2 |  |  |
| 7(i) | let $\mathrm{P}(2,4,6)$ all $=p$ then $\mathrm{P}(1,3,5)$ all $=2 \mathrm{p}$ | 1 | M1 | Using $\mathrm{P}($ even $)=2 \mathrm{P}$ (odd) or vice versa oe |
|  | $3 p+6 p=1$ | 1 | M1 | Summing $\mathrm{P}($ odd + even $)$ or $\mathrm{P}(1,2,3,4,5,6)=1$ |
|  | $p=1 / 9$ so prob ( 3 ) = 2/9 (0.222) | 1 | A1 | Correct answer |
|  |  | 3 |  |  |
| 7(ii) | $\mathrm{P}(5,5,6)=2 / 9 \times 2 / 9 \times 1 / 9 \times{ }^{3} \mathrm{C}_{2}$ | 2 | $\begin{aligned} & \text { M1 } \\ & \text { M1 } \end{aligned}$ | Mult three probs together <br> Mult by 3 oe ie summing 3 options |
|  | $=4 / 243$ (0.0165) | 1 | A1 | Correct answer |
|  |  | 3 |  |  |


| Question | Answer | Marks | Partial Marks | Guidance |
| :---: | :---: | :---: | :---: | :---: |
| 7(iii) | $\mu=100 \times 1 / 3=33.3, \sigma=100 \times 1 / 3 \times 2 / 3=22.2$ | 1 | B1 | Unsimplified 100/3 and 200/9 seen |
|  | $\mathrm{P}(x \leqslant 37)=\mathrm{P}\left(z \leqslant \frac{37.5-\frac{100}{3}}{\sqrt{\frac{200}{9}}}\right)=\mathrm{P}(z \leqslant 0.8839)$ | 3 | $\begin{aligned} & \text { M1 } \\ & \mathbf{M 1} \\ & \mathbf{M 1} \end{aligned}$ | Standardising need sq rt 36.5 or 37.5 seen correct area using their mean |
|  | $=0.812$ | 1 | A1 | Correct answer |
|  |  | 5 |  |  |

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